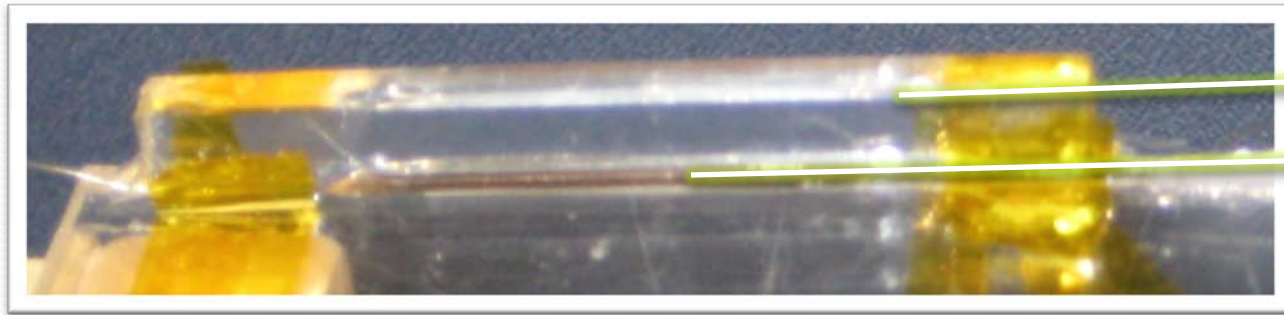


# ANNUAL PERFORMANCE MODEL OF CONCENTRATING COMPOUND PARABOLIC CONCENTRATOR INTEGRATED PHOTOVOLTAICS

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Truncated CPC

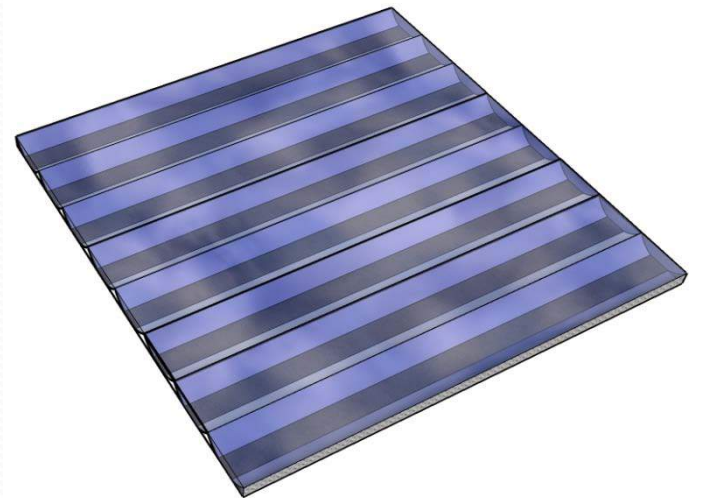
PV strip

## Objective:

- Developing and testing a methodology to quantify the power produced by a concentrating compound parabolic collector integrated PV (CPV).
- At finding the optimal orientation of the CPV.

# Concentrating Photovoltaics (CPV)

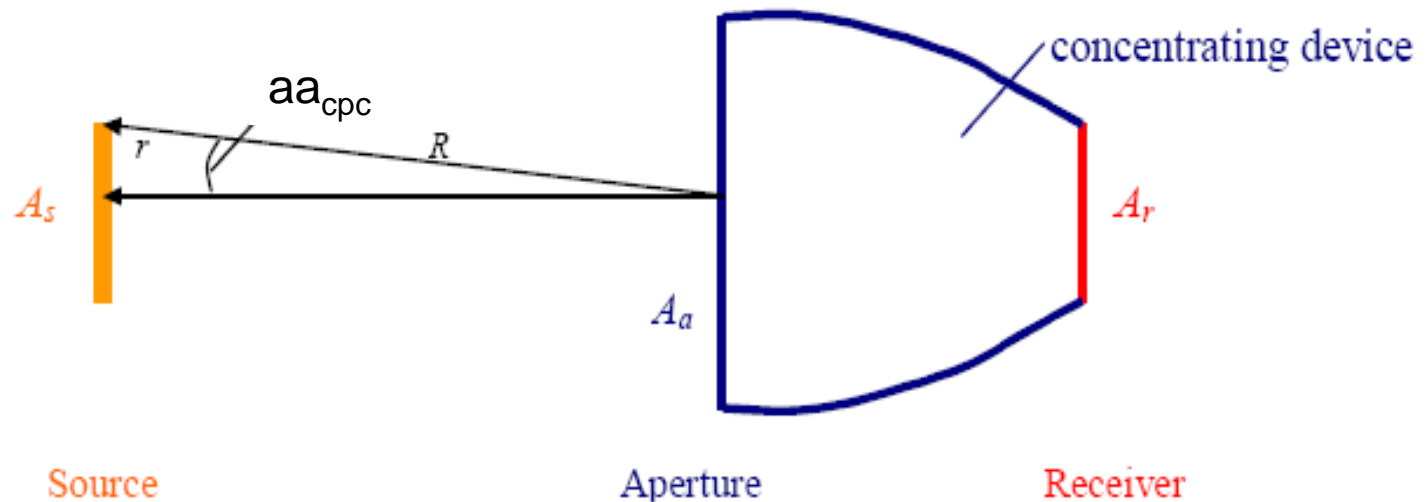
- Use less PV material still providing a reasonably high power output.
- Cost effective, require lower capital investment, and have the potential for large scale solar power generation.



# Compound Parabolic Collector

$$\text{Acceptance angle} = \text{aa}_{\text{cpc}} = \sin^{-1} \left( \frac{1}{\text{CR}} \right)$$

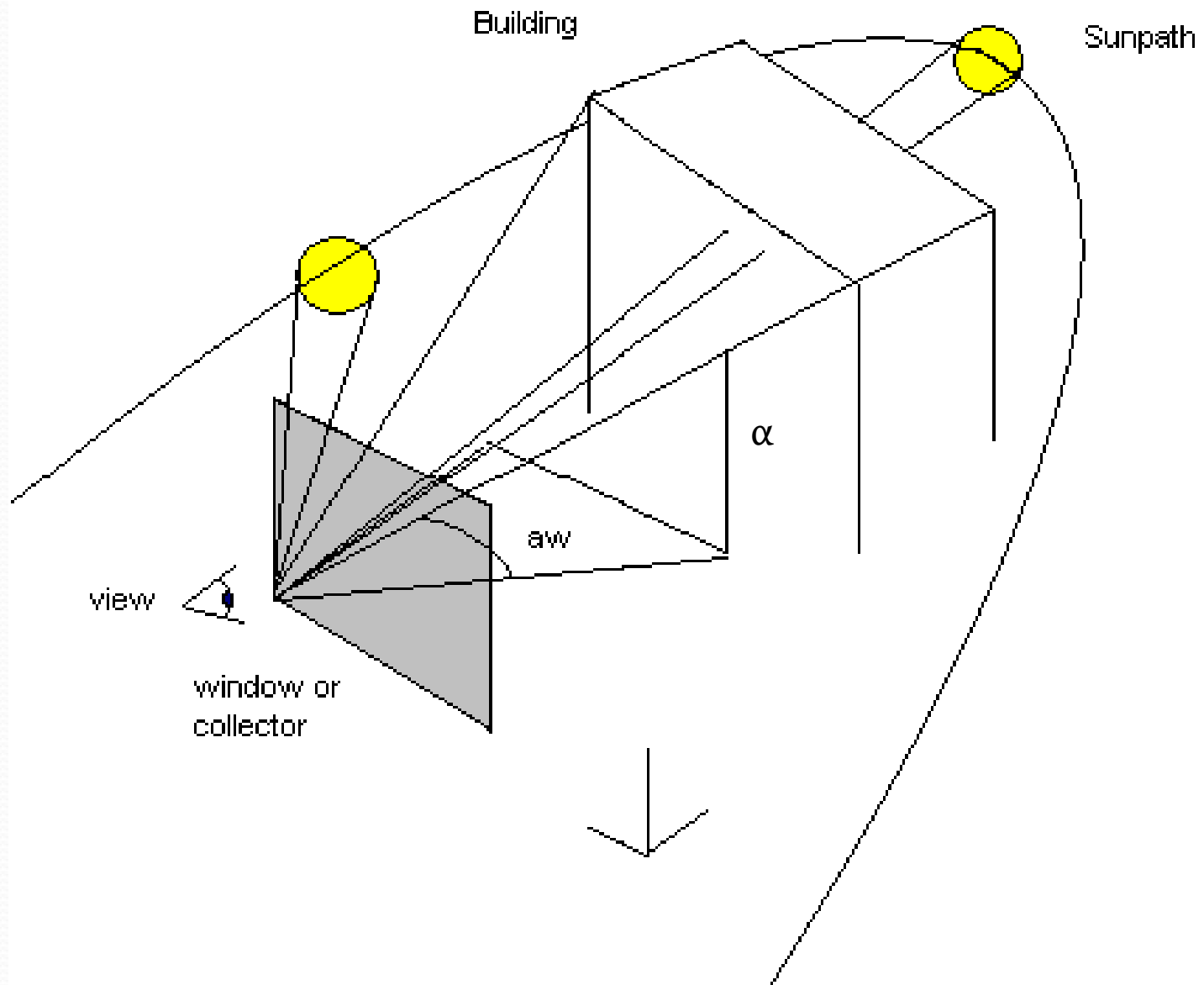
$$\text{Concentration Ratio} = A_a / A_r$$



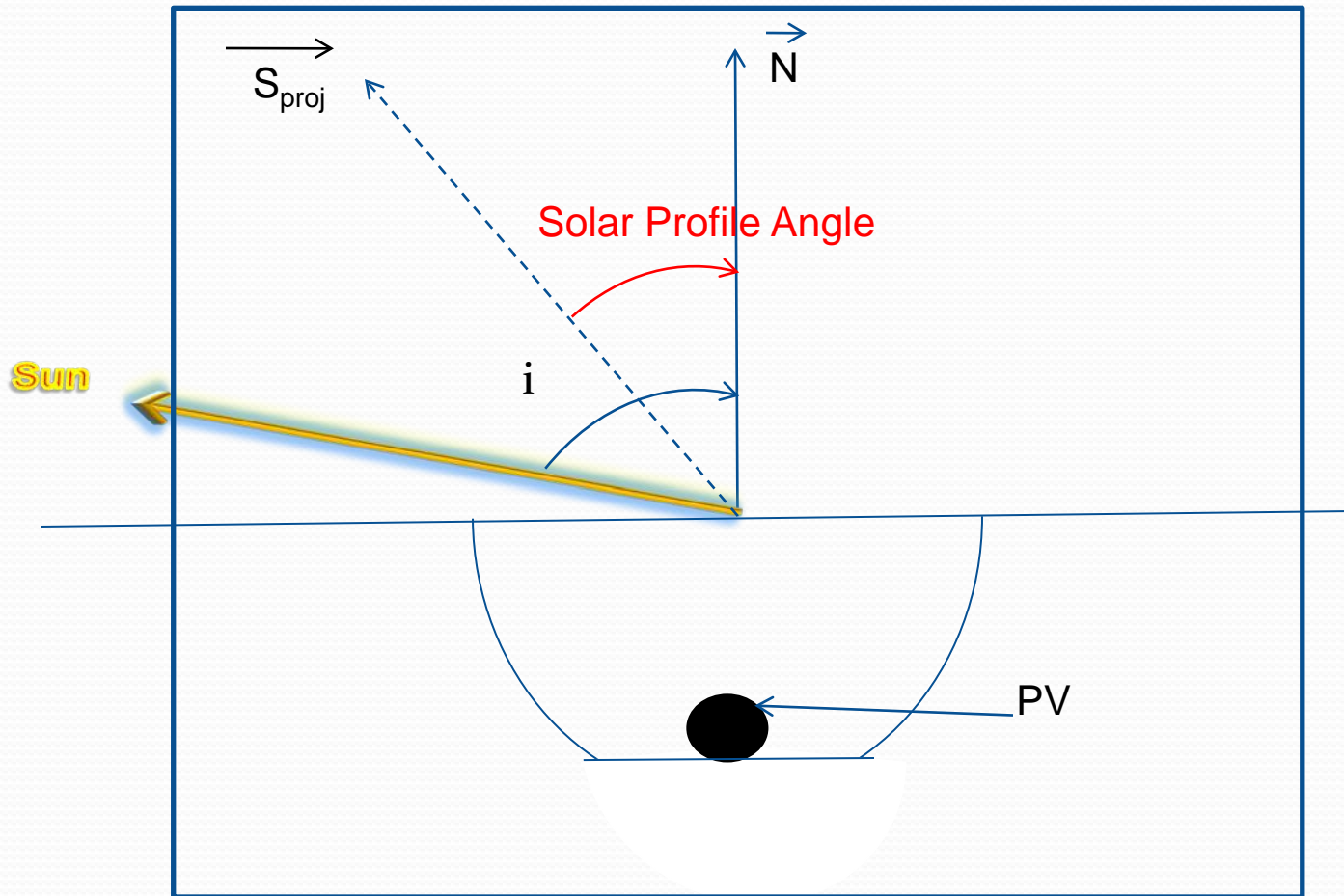
# Solar Profile Angle

Solar profile angle of the incident beam radiation on a receiver plane is the projection of the solar altitude angle on a vertical plane perpendicular to the plane in question.

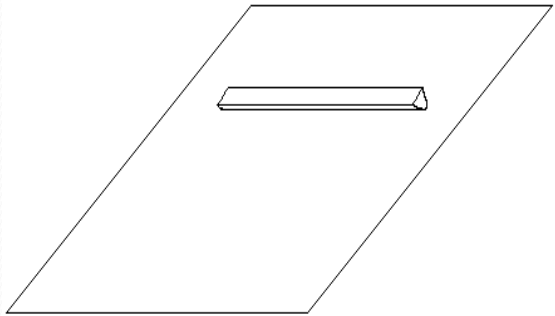
$$\theta_{p1} = \tan^{-1}(\tan(z) * \cos(\alpha_s - \alpha_w))$$



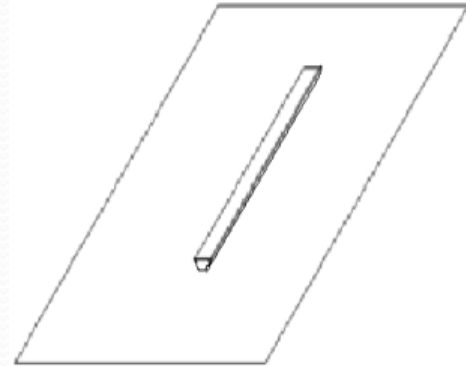
# Solar Profile Angle & CPV



# A tale of 2 directions..



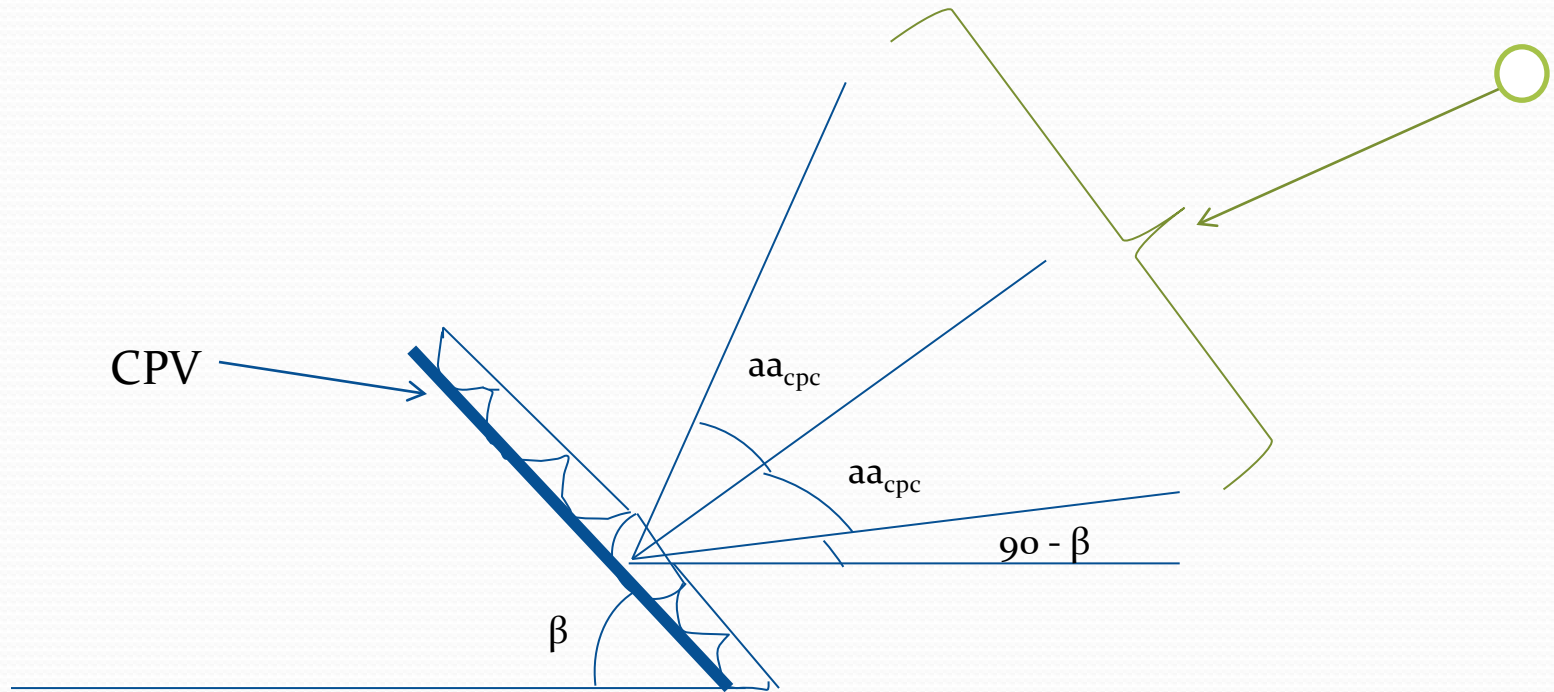
Orientation-1 (east-west)



Orientation-2 (north-south)



# Orientation-1 (East-West)

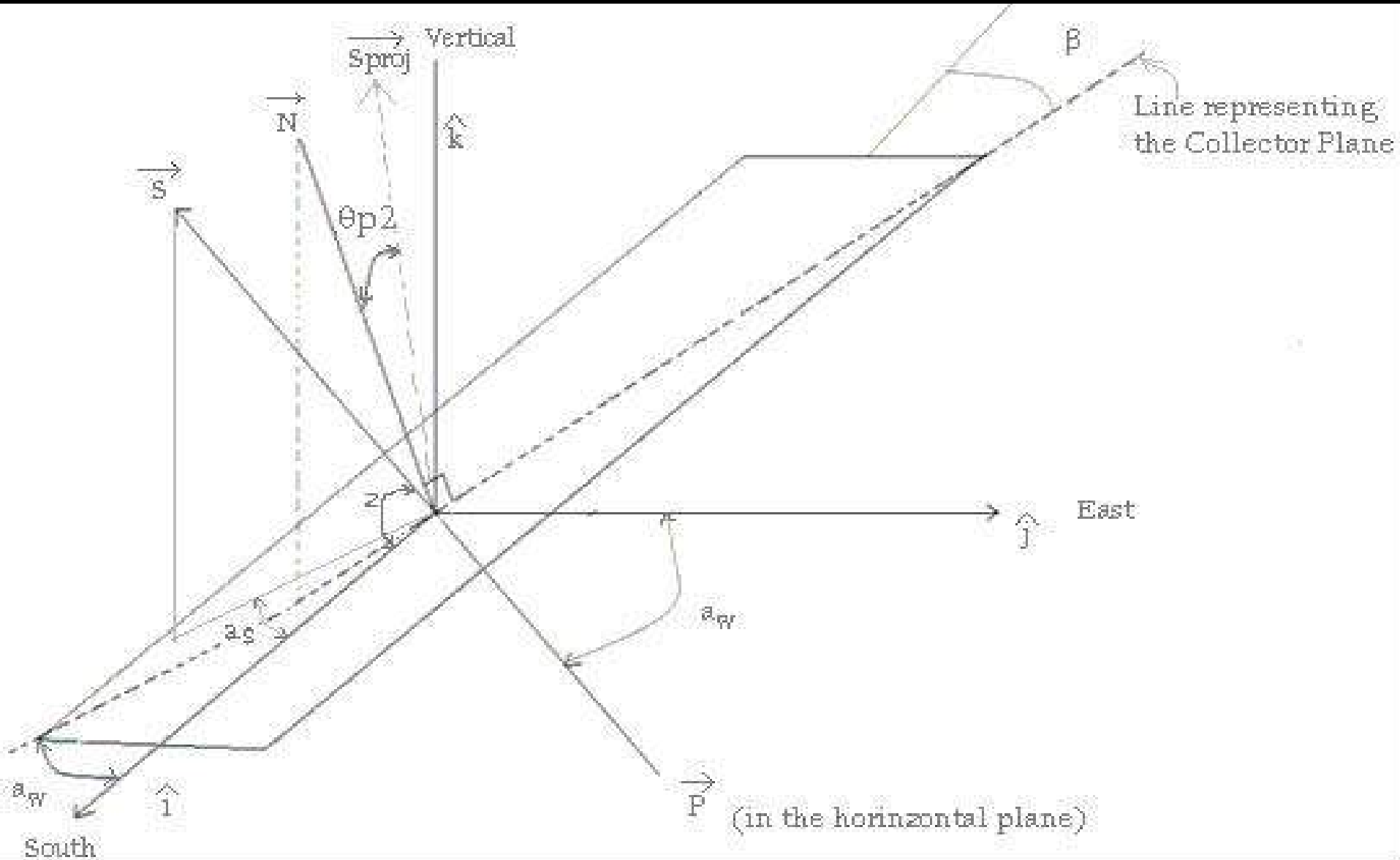


If,  $\alpha > 0$

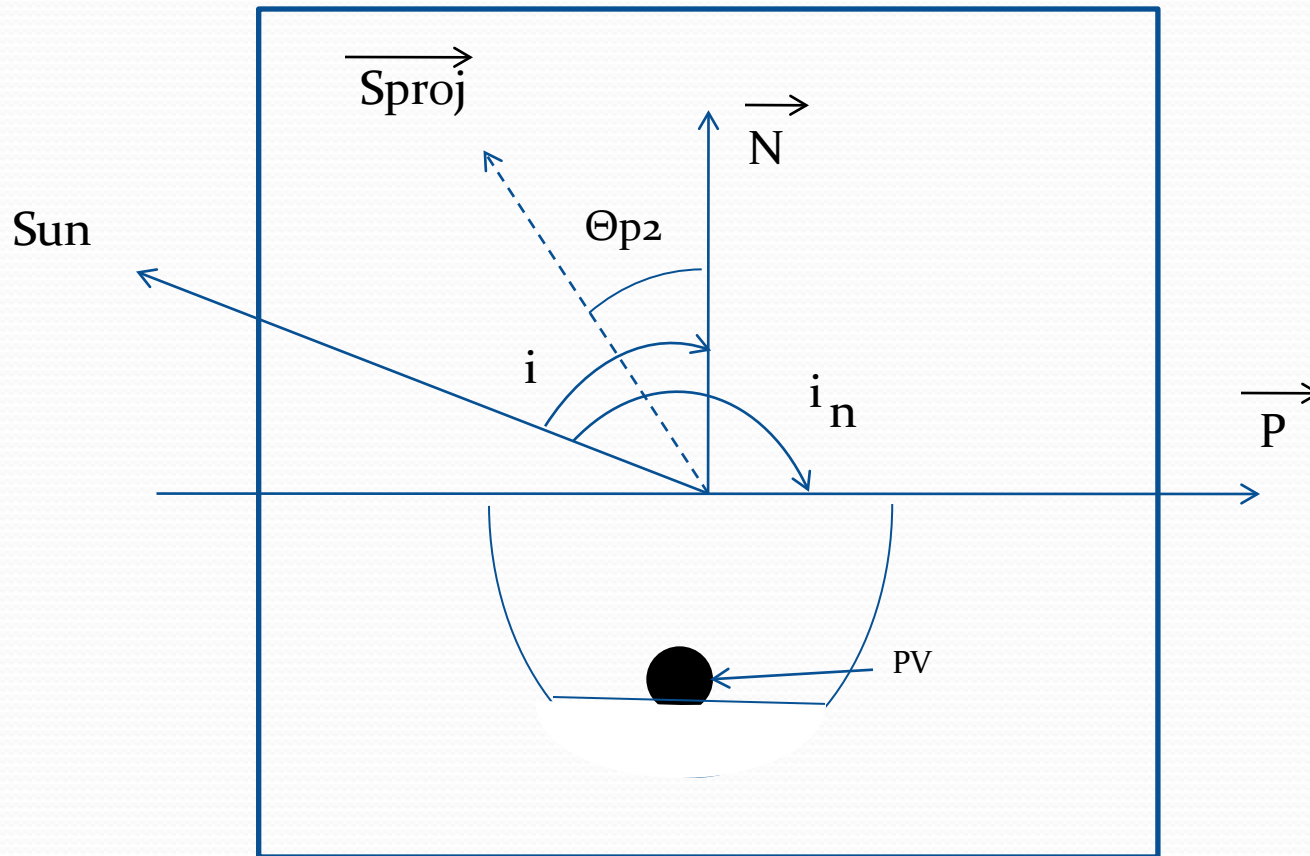
$$(90 - \beta - 2 * aa_{cpc}) < \theta_{p1} < (90 - \beta + 2 * aa_{cpc})$$

Then, Beam Irradiation enters the CPV. Otherwise, it does not!

# Orientation-2 (North-South)



# Profile View in Orientation-2 (North-South)



# Vector geometry to the rescue!

$$\tan \theta_{p2} = \frac{\vec{S} \cdot \vec{N}}{\vec{S} \cdot \vec{P}} = \frac{\cos i}{\cos i_N}$$

$$\theta_{p2} = \tan^{-1} \left( \frac{\cos i}{\cos i_N} \right)$$

$$\cos i_N = \cos a_g \sin z \sin a_w + \cos a_w \sin a_g \sin z$$

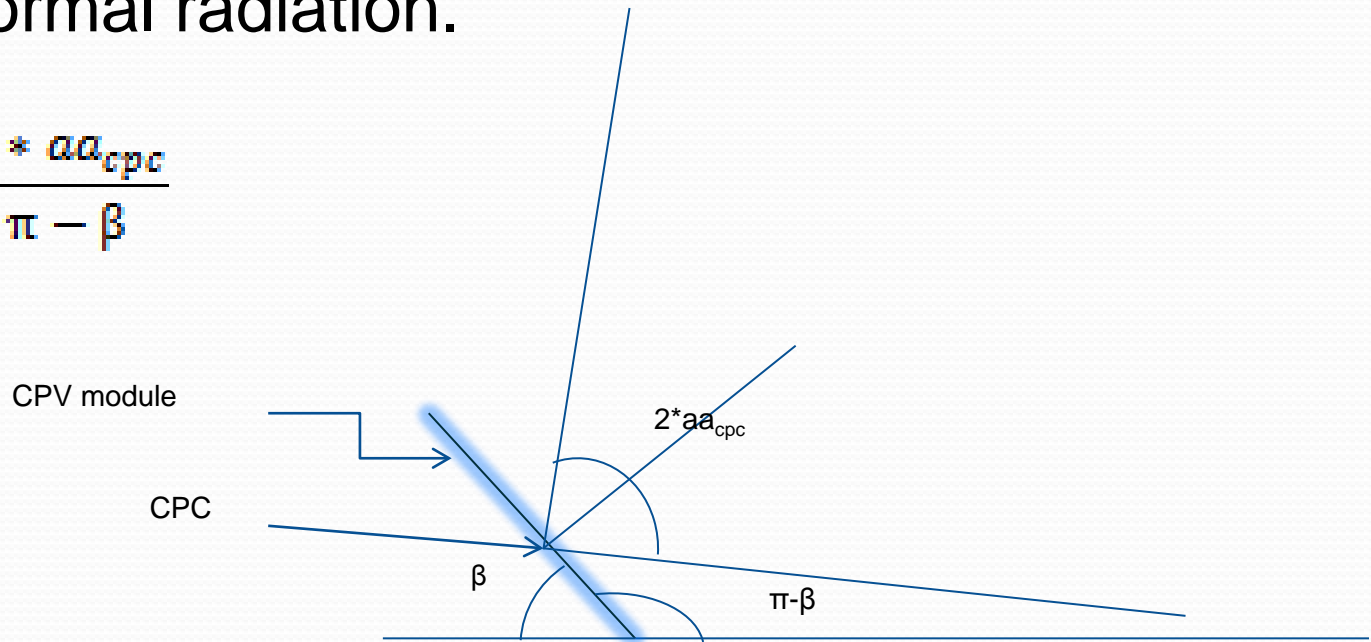
If,  $\theta_{p2} > a_{cpc}$   Beam irradiation hits the PV at the bottom;

Else, No Beam irradiation entering the CPV!

# Diffuse radiation

We quantified it to be a fraction of the global diffuse radiation and the ground reflected component of the beam normal radiation.

$$\text{fraction} = \frac{2 * aa_{cpc}}{\pi - \beta}$$



This is geometrically valid for slopes less than 90 degrees, which seems reasonable.

# Methodology

Database of hourly irradiation was taken from NSRDB, TMY3 records for Concord, NH  
Beam Incident Irradiation is estimated by using the following equation,

$$I_{cpv} = I_{beam} + [\overline{R}_d \cdot I_D + \overline{R}_r \cdot I_{beam}] \cdot \text{fraction}$$

Where,

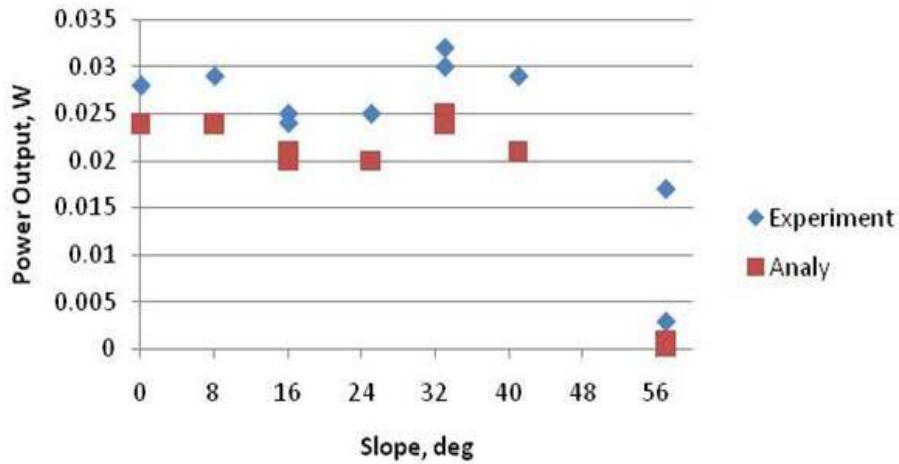
$$\overline{R}_d = \left( \frac{1 + \cos \beta}{2} \right) \quad \overline{R}_r = \rho_g \cdot \left( \frac{1 - \cos \beta}{2} \right)$$

Power output is estimated by,  $P = I_{cpv} \cdot A_{lens} \cdot \eta \cdot \tau \cdot (1 + \Delta P)$

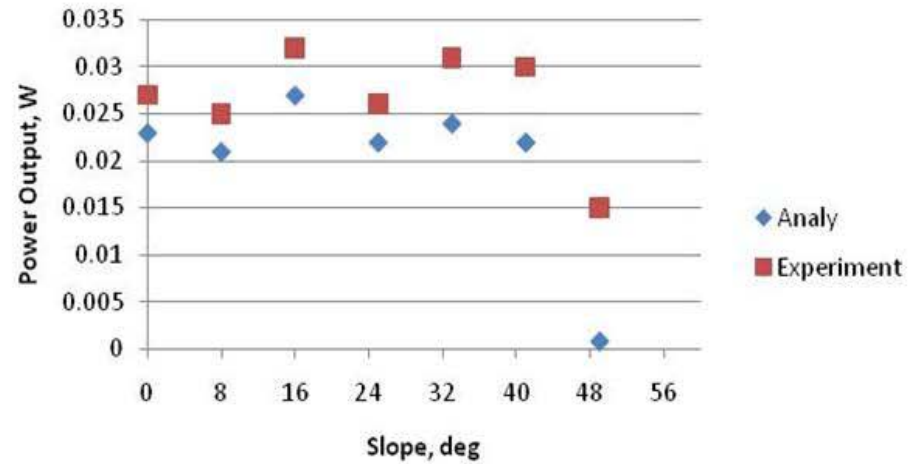
Temperature effects were considered,  $\Delta P = \Delta T_c \cdot \Delta P\%$

# Experimental Verification

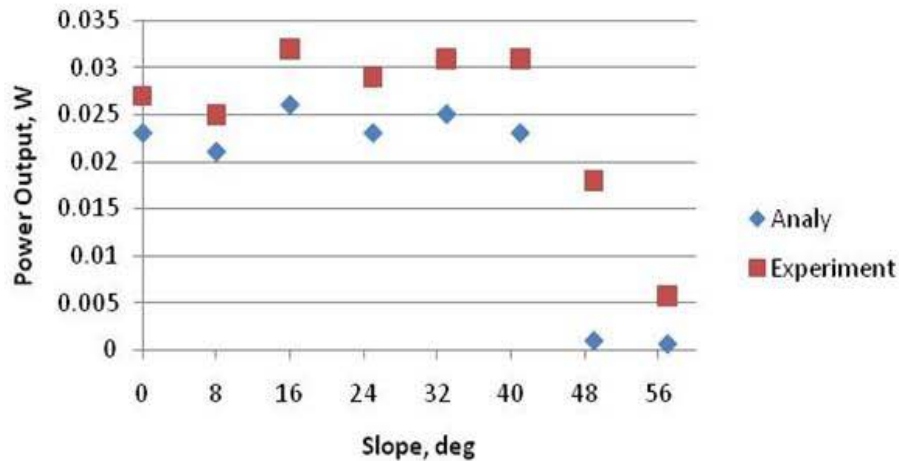
## Azimuth 20°



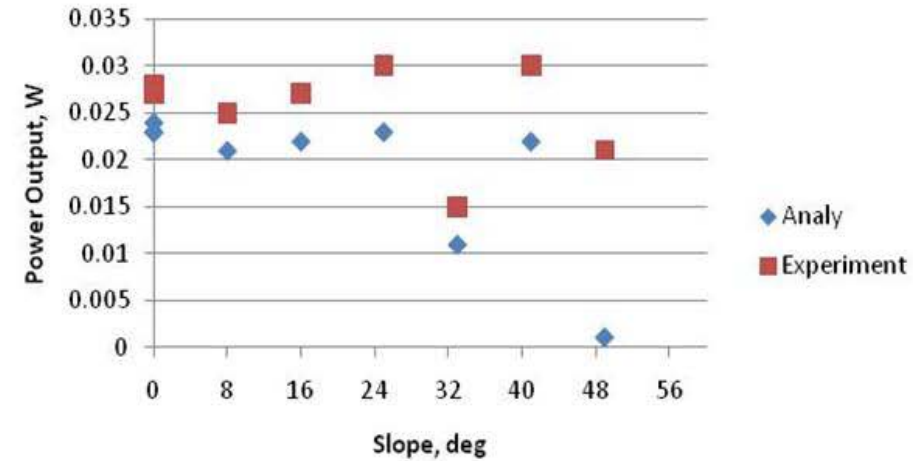
## Azimuth 30°



## Azimuth 50°



## Azimuth 60°

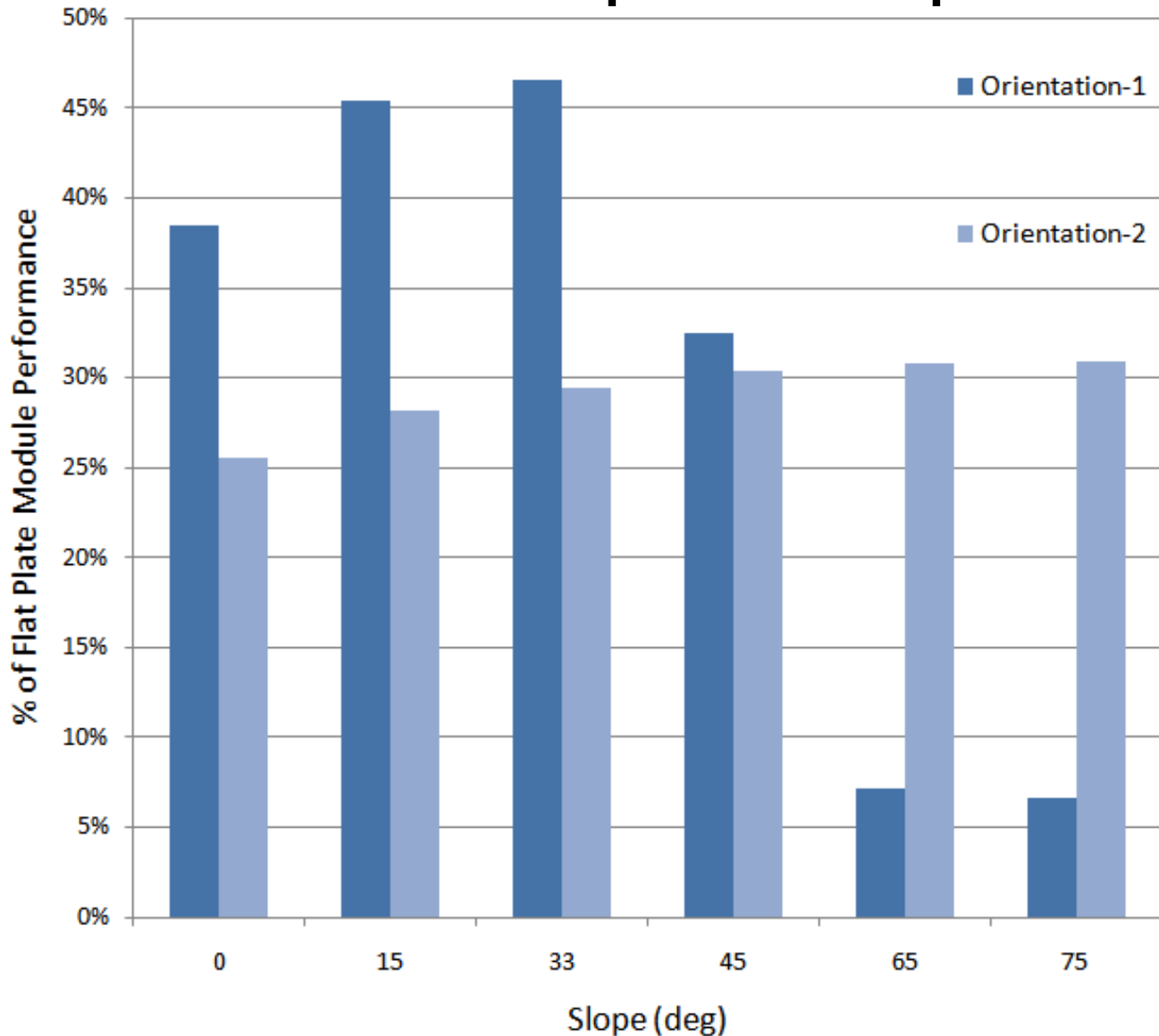


# Difference b/w Analytical & Experimental Results

- Discretization uncertainty, due to the very small current output from the experimental module.
- Moreover, at higher collector slopes where the profile angle is outside of the acceptance range, the current produced is extremely small resulting in higher discretization uncertainty.
- Irradiation entering from the side of the CPC has not been considered.



# Annual Power Output Comparison



Note: Assuming equal aperture area of Flat Plate Module and the CPV

# In Conclusion..

The annual model demonstrates that optimal performance is attained at low roof slopes while the CPV is aligned “east-west” in orientation-1.

At higher collector slopes as required in building elements, CPV aligned “north-south” in Orientation-2 offers better performance.

# Recommendations

- Incorporating the irradiation that enters through the side of the CPC.
- A module could be built and tested instead of a cell, for less discretization error.
- More tests could be conducted on the orientation-2.
- Field tests for prolonged periods of time could provide useful data on temperature effects.
- Transmittance as a function of incidence angle could be investigated.



Thank You for your attention!



Any questions?